ACCURACY OF GEODETIC SURVEYS IN CADASTRAL REGISTRATION OF REAL ESTATE: VALUE OF LAND AS DETERMINING FACTOR

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Abstract. For millennia, the geodesic industry has improved methods and technologies for obtaining information on location of objects on the Earth's surface, the key task being to improve the accuracy and reliability of measurements. At the same time, in recent decades, the rapid development of positioning technologies based on satellite radio navigation systems has created prerequisites for a situation, where the acceptable accuracy of determining the geodetic characteristics of real estate becomes quite affordable even using non-specialized geodetic equipment, including personal mobile devices. The article shows that the error in determining the area of land for registration of rights to real estate has its own "cost", which depends on the value of real estate in the area of survey. By the example of model sites, it is shown that further improvement of the accuracy of engineering surveying to determine the spatial characteristics of real estate objects would be economically feasible only if the cost of geodetic surveys (including the cost of purchasing new geodetic equipment, payment for labor of specially trained engineers, additional technical services and etc.) will not exceed the "cost of error" to determine the area of the site. Using the example of Ukraine, it is shown that the most accurate geodetic surveys (determining turning points of land borders with an accuracy of more than 0.02 m) are economically feasible only when the market value of a land plot exceeds USD 208 per square meter.

Keywords: accuracy, surveys, geodesy, value, land, cadastre.

Introduction

At the current pace of development of satellite and network technologies, the role of man in performing topographic and geodetic surveys in the field of land management is decreasing. In particular, today the use of GNSS-technologies has practically replaced the basic methods of creating geodetic networks for various geodetic works (triangulation, trilateration, polygonometry), including determination of the coordinates of the turning points of the land plot during cadastral surveys and land inventories, establishment of boundaries of the land plot on the ground.

Existing differentiation of accuracy and cost of topographic and geodetic surveys, in particular, for the purpose of inventory of land [1], creates preconditions for further research in the field of engineering economics, namely:

- definition of the dependence of the cost of topographic and geodetic works in the field of land management on the accuracy of these works;
- estimation of the efficiency of using modern satellite technologies for the purpose of the real estate cadastre (especially, when installing (fixing) the turning points of the land plot within the permissible error of 0.5 meters), and determining the prospects for using the mobile gadgets (smartphones, tablets, etc.) for these purposes;
- establishment of acceptable accuracy of topographic and geodetic surveys in the real estate cadastre depending on the market value of the land plot.

Problems of establishing the requirements for the accuracy of land cadastral papers were undertaken by various scientists, in particular, Zhilinsky (2013) tried to investigate the influence of economic factors on the accuracy of geodetic measurements during cadastral works, and established, in the conditions of the city of Lviv, the size of the error of determining the area of land in cash equivalent [2].

Petrov and Tserklevich (2011) [3] found that the change in the mean square error (MSE) of determining the coordinates of the points of land plot boundary proportionally affects the change in the MSE of their area. Kristin M. Stock (1998) [4] carried out a sociological study, in which she insisted on the accuracy of establishing the boundaries of the land in the countryside. It is determined that the overwhelming majority of the surveyed landowners, including the local authorities and relevant municipal organizations in the study area, require the maximum accuracy of establishing the boundaries of the land plot in the range of ± 0.2 and ± 0.5 m.

An analysis of the historical stages of development of technologies in geodesy and their impact on the accuracy of land cadastral surveys is presented in the scientific publication Belle A. Craig and Jerry L. Wahl (2003) [5].

At the same time, Tim Burch (2017) in his article draws attention to the fact that the development of modern GNSS technologies reduces the relevance of the classical study of geodetic surveying methods and minimizes the role of a certified geodesist specialist in the implementation of various types of land cadastral work [6].

Materials and methods

The current state of the development of GNSS technologies allows to get the coordinates of the points with the maximum possible accuracy of 1 meter (raw data by satellite observations) even under favorable observation conditions (PDOP, GDOP, etc.).

It is clear that for the purpose of land management, the accuracy of positioning in 1 m is not permissible, such circumstances directly influenced the development of appropriate positioning methods for achieving higher accuracy in determining the planned height position of the reference points: the static method; fast static; RTK – Real Time Kinematics.

However, the use of RTK mode involves receiving amendments from the base station, that is, from the receiver, which is set at a point with a known (true) coordinate, points of the state geodetic network. To date, such base stations have permanent stations.

In Ukraine, the main organizations that hold national networks of GNSS permanent stations are private companies, as described in Table 1.

Table 1

Name	System Solutions	TNT TPI GNSS Network	Zak Pos
1	2	3	4
GNSS brand equipment offered by the company	Leica Geosystems	TOPCON	Trimble
	Cost of services:		•
	Real-time positioning (RTI	K)	
1 hour	-	0.4 USD	-
1 minute	0.1 USD RINEX & Virtual RINEX – 0.04 USD	0.02 USD	0.06 USD
1 month subscription	-	21.3 USD	41.3 USD
Subscription 3 months	207 USD	57 USD	-
Annual subscription	571.8 USD	202.7 USD	412.5 USD
Post processing raw file in RINEX format	1.78 USD	-	-
Equipment rental	1 day – 35.6 USD·day ⁻¹ ; 2-6 days – 28.4 USD·day ⁻¹ ; 7-13 – days 27.0 USD·day ⁻¹ ; 2 weeks – 311.0 USD; month – 604.6 USD	Do not provide such services (only the sale of equipment)	Do not provide such services
Precision farming from 248.9 USD		from 32.0 USD	-

Analysis of private permanent networks to provide GNSS surveillance data adjustment in Ukraine

The above information was taken into account in further development of the estimate of the cost of geodetic works in establishing the boundaries of the land plot (Table 2).

							Table 2
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Calculation of the cost of geodetic works in relation to fixing the bound	aries of the land plot
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		_			1	
Level of acceptable accuracy for the purpose of inventory of land		I a	b	Π	III	
		up to 2 cm	2-10 cm	10-20 cm	20-50 cm	
GNSS	Type of the most effective method for achieving the correct accuracy	Static	Real Time Kinematic (RTK)		RTK	
technology	Geodetic binding	State geodetic network (reference points)	Reference points + state geodetic network for calibration	ints + state points + state letic network geodetic network		
Estimate of the cost of	Cost of data on the coordinates of the item of the state geodetic network (reference points) *	3×5.3 USD = 16 USD	5.3 USD	5.3 USD	-	
geodetic works in relation to the establishment of the boundaries of the land plot ***	Rent for the required geodetic equipment **	Base + Rover (GNSS Leica GS08Plus (GS12) + CS10) – 71.1 USD \cdot day ⁻¹ ; Tacheometer (Leica TS09plus R500 (5")) – 35.6 USD \cdot day ⁻¹ ;	Rover (GNSS Leica GS08Plus (GS12) + CS10) - 35.6 USD·day ⁻¹ ;	Rover (GNSS Leica GS08Plus (GS12) + CS10) - 35.6 USD·day ⁻¹ ;	Rover (GNSS Leica GS08Plus (GS12) + CS10) - 35.6 USD·day ⁻¹ ;	
	Cost of receiving RTK corrections ** Total	- 122.7 USD	$207.0 \text{ USD per 3} \\ \text{months} \rightarrow \\ 1 \text{ day} = 2.3 \text{ USD} \\ 43.2 \text{ USD}$	2.3 USD·day ⁻¹ 43.2 USD	2.3 USD · day ^{−1} 37.9 USD	
Number of employees		2	1	1	1	
Cost of determining the boundaries of the land plot		32.0 USD per point (at the same time the minimum cost of departure of a surveyor is 71.2 USD)	10.1 USD per point (at the same time the minimum cost of departure of a surveyor is 53.3 USD)	10.1 USD per point (at the same time the minimum cost of departure of a surveyor is 53.3 USD)	7.1 USD per point	

* - according to the Research Institute of Geodesy and Cartography [7];

** – according to System Solutions (Table 1);

*** – in the indicated estimate there are no calculations for logistics costs, since these data are individual for each object

In Ukraine, in accordance with the Resolution of the Cabinet of Ministers of Ukraine dated May 23, 2012, No. 513 "On Approval of the Procedure for Land Inventory Management", the error of determining the turning points of land plots relative to the nearest points of the state geodetic network should not exceed [8]:

- in Kyiv, Sevastopol and cities of regional subordination 0.1 meters;
- in other cities and towns 0.2 meters;
- in villages 0.3 meters;
- outside of settlements 0.5 meters.

The stated allowable accuracy of determining the position of the turning points of the land plot on the ground has been based on the analysis of the cost of topographic and geodetic works, namely:

- when choosing effective methods of creating a reference geodetic network the most accurate differential method in the application of GNSS technologies is the "Static" method, which allows to determine the position of points (sampling ground) to 1 mm, and then, with the help of geometry, fix the boundaries of the land plot to within 10-20 mm; At the same time, the application of the polygonometric method, in modern technologies, is inappropriate, except for the presence of dense building, densely planted areas forest arrays, etc.
- in determining the required geodetic equipment and the number of performers. According to the above methods, for the purpose of achieving the appropriate precision, we have identified the kits of the required equipment and presented their market lease payment [9], determined on the basis of (Table 2) the amount of payment for receiving RTK corrections and the cost of coordinates of the outgoing points of the State Geodetic Network [7].

It is important to note that at the time of drafting the estimate of the cost of land cadastral works for fixing the boundaries of the land, the rate of USD – 28.12 UAH to USD (official data of the National Bank of Ukraine as of 18.09.2018), and the average wage in Ukraine – 7621 UAH per month (271 USD) [10].

Thus, from the above calculations in Table 3, we have the cost of geodetic works for fixing the boundaries of the land plot with an accuracy of I – 45.27 % of the average monthly salary in Ukraine and requires two executors, and II – 15.94 % (one performer), III – 13.97 % (one performer).

In fact, we have established a direct correlation between the accuracy and cost of topographic and geodetic works in relation to fixing the boundaries of the land plot on the ground, that is, with "higher precision" "higher price".

Results and discussion

According to the results of our analysis, we can further speak about the dubious necessity of conducting high-precision geodetic surveys (in view of their high cost) for the purpose of land cadastre, in particular, inventory of land and the establishment of boundaries of land in the area. We believe that achieving high accuracy in conducting geodetic works in the field of land cadastre is an indirect necessity, which should be determined based on the market value of the surveyed land plot.

Subsequently, our studies concerned the definition of acceptable accuracy of land cadastral work, which in our opinion, should be determined on the basis of economic factors. That is, in order to find out the expediency of implementing high-precision topographic and geodetic works in the field of land cadastre, it is necessary to compare the error of the definition of the area and market value of the corresponding land with the cost of geodetic works.

Conditionally, if a plot of land has the shape of a rectangle, which sides a and b are defined with average square errors m_a and m_b accordingly, then the error of determining the area of the land S, according to the theory of errors, will be determined by the formula

$$m_s^2 = \left(\frac{\partial S}{\partial a}\right)^2 \times m_a^2 + \left(\frac{\partial S}{\partial b}\right)^2 \times m_b^2 \tag{1}$$

We find partial derivatives:

$$\frac{\partial}{\partial a} = b; \frac{\partial}{\partial b} = a \tag{2}$$

Having defined partial derivatives we have the general formula for determining the error of the area of the land plot of a rectangular shape with certain errors in measuring the length (m_a) and width (m_b) :

$$m_s^2 = b^2 \times m_a^2 + a^2 \times m_b^2 \tag{3}$$

Thus, mathematically proved and quite understandable is the fact that the error in the area of the land will be directly affected by the error of determining the linear elements (boundaries) of the land.

Consequently, in general, if the value of *f* is expressed in terms of independently measured values x_i ($i = 1, \bar{n}$) – the coefficients, then the mean square error m_f of the value of *f* will be

$$m_{f} = \pm \sqrt{\sum_{i=1}^{n} a_{i}^{2} \times m_{i}^{2}} = \pm \sqrt{\left[a^{2} \times m^{2}\right]}$$
(4)

If the measurements x_i ($i = 1, \bar{n}$) are equivalent and $m_1 = m_2 = ... = m_n = m$, then:

$$m_f = \pm m \sqrt{\left[a^2\right]} \tag{5}$$

The resulting formula for the mean square error is obtained from the relation::

$$m_F^2 = \left(F_x^{'}\right)_0^2 \times m_x^2 + \left(F_y^{'}\right)_0^2 \times m_y^2 + \dots + \left(F_u^{'}\right)_0^2 \times m_u^2, \tag{6}$$

and expressions for partial derivatives of f for arguments X_i :

$$\frac{\partial f}{\partial x_i} = a_i, \left(i = \overline{1, n}\right). \tag{7}$$

At the same time, the function to determine the area of the land plot with known coordinates of the turning points will have the following form:

$$S = \frac{1}{2} \sum_{i}^{n} X_{i} (Y_{i+1} - Y_{i-1})$$
(8)

In this case, the margin of error in determining the area of the land will be determined by the following formula:

$$m_{s} = \sqrt{1/4\sum_{i=1}^{n} \left\{ \left(X_{i+1} - X_{i-1}\right)^{2} \times m_{y}^{2} + \left(Y_{i+1} - Y_{i-1}\right)^{2} \times \right\} m_{x}^{2}}$$
(9)

where m_x, m_y – mean square error of the coordinates of the turning points of the land plot.

In the course of our study, we determined the margin of permissible error in determining the area of land. To do this, simulation was done of the size of the land plot, which in shape corresponded to the figure of a rectangle, with different perimeters (lengths) of the parties in the range from 0.01 ha to 5 hectares. The average quadratic error in determining the position of turning points was determined in accordance with the Resolution of the Cabinet of Ministers of Ukraine dated May 23, 2012 No. 513 [8] (Table 3).

Table 3

		Average	Calculation of the error of the area of land, m ²							
	Placement of land	square error of Land area, ha								
		determining	5	1	0.5	0.25	0.10	0.01		
N⁰	[8]	the position of			Perime	ter, m				
	[0]	the turning								
		points of the	895	400	283	200	128	40		
		land (m) [8]								
1	2	3	4	5	6	7	8	9		
1	Kiev, Sevastopol city and cities of regional	to 0.02 (high precision)	17.9	8	5.66	4	2.56	0.8		
	subordination	0.1	89.5	40	28.3	20	12.8	4		
2	In other cities and towns	0.2	179	80	56.6	40	25.6	8		
3	in villages	0.3	268.5	120	84.9	60	38.4	12		
4	Outside of the settlement	0.5	447.5	200	141.5	100	64	20		

Calculation of the error of the area of land

Thus, we have calculated the errors in determining the area of land ($S_1 = 0.01$ ha; $S_2 = 0.10$ ha; $S_3 = 0.25$ ha; $S_4 = 0.50$ ha; $S_5 = 1.00$ ha; $S_6 = 5.00$ ha), taking into account the errors of the position of the turning points ($m_1 = 0.02$ m; $m_2 = 0.1$ m; $m_3 = 0.2$ m; $m_4 = 0.3$ m; $m_5 = 0.5$ m) (Table 3).

The next stage of our study was to determine the acceptable accuracy of establishing the boundaries of the land due to its market value. Taking into account the data of Table 2 (cost of topographic and geodetic works) and Table 3 (size of errors in land parcels) and taking into account the norms of the current legislation [8], we determined the minimum size of the land values to achieve cost-effective implementation of high-precision geodetic measurements in the field of inventory of land (Table 4).

Table 4

I – Economic feasibility of carrying out topographic and geodetic works with high accuracy						
1-a) Mean square error of determination of the position of the turning points of the land plot to 0.02 m						
Land area, ha	5.00	1.00	0.50	0.25	0.10	0.01
Error in the area of the land, m ²	17.90	8.00	5.66	4.00	2.56	0.80
Market value of land to achieve economic effect, 1 m ² ·USD ⁻¹	9.28	20.76	29.34	41.52	64.87	207.5 9
II – Economic feasibility of carrying out topogr	aphic and	geodetic w	vorks with	the correc	t accurac	y
1) Mean square error of the definition of the po	sition of th	e turning j	points of tl	he land plo	ot of 0.1 1	n
Land area, ha	5.00	1.00	0.50	0.25	0.10	0.01
Error in the area of the land, m ²	89.50	40.00	28.30	20.00	12.80	4.00
Market value of land to achieve economic effect, 1 m ² ·USD ⁻¹	0.96	2.16	3.05	4.31	6.74	21.56
2) Mean square error of the definition of the position of the turning points of the land plot of 0.2 m						
Land area, ha	5.00	1.00	0.50	0.25	0.10	0.01
Error in the area of the land, m ²	179.00	80.00	56.60	40.00	25.60	8.00
Market value of land to achieve economic effect, 1 m ² ·USD ⁻¹	0.48	1.08	1.52	2.16	3.37	10.78
3) Mean square error of the definition of the po	sition of th	e turning j	points of tl	he land plo	ot of 0.3 1	n
Land area, ha	5.00	1.00	0.50	0.25	0.10	0.01
Error in the area of the land, m ²	268.50	120.00	84.90	60.00	38.40	12.00
Market value of land to achieve economic effect, 1 m ² ·USD ⁻¹	0.32	0.72	1.02	1.44	2.25	7.19
4) Mean square error of the definition of the position of the turning points of the land plot of 0.5 m						
Land area, ha	5.00	1.00	0.50	0.25	0.10	0.01
Error in the area of the land, m ²	447.50	200.00	141.50	100.00	64.00	20.00
Market value of land to achieve economic effect, 1 m ² ·USD ⁻¹	0.19	0.43	0.61	0.86	1.35	4.31

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Economic feasibility	y of implementation	n or topographic an	a geodetic works

That is, we justified the marginal market value of the land plot, in which the implementation of topographic and geodetic works of appropriate accuracy will be economically feasible in the field of land cadastre.

From the data obtained (Table 4), it is safe to say that precise geodetic work (determination of the position of the turning points of the land plot to 0,02 m), in view of their high cost, in comparison with others, is expedient to carry out in cases, where the market value of 1 m² the land plot reaches $207.59 \text{ m}^2 \cdot \text{USD}^{-1}$ when establishing boundaries of a land plot with a total area of 0,01 hectares; $64.87 \text{ m}^2 \cdot \text{USD}^{-1}$ – land area of 0.10 hectares; $41.52 \text{ m}^2 \cdot \text{USD}^{-1}$ – land area of 0.25 hectares; $29.34 \text{ m}^2 \cdot \text{USD}^{-1}$ – land area of 0,50 hectares; $20.76 \text{ m}^2 \cdot \text{USD}^{-1}$ – land area of 1.00 hectares; $9.28 \text{ m}^2 \cdot \text{USD}^{-1}$ – land area of 5.00 hectares.

At the same time, given the high cost of high-precision geodetic equipment and the rapid development of modern telecommunication technologies (smartphones, tablets) with the support of positioning technologies (GNSS-technology), it is extremely important to provide a scientific and practical evaluation of the use of these electronic gadgets in the implementation of land -capital works (surveying, inventory of land, establishing boundaries of the land plot on the ground), especially when the marginal error of the performance of these works must be achieved in the range 20-50 cm,

depending on the location of the land (in other cities and towns -0.2 meters, in villages -0.3 meters, outside the settlements -0.5 meters [8]).

For example, to date, Xiaomi has been developed and offered to users, the new flagship Xiaomi Mi 8, equipped with a dual-frequency GPS module L1 + L2. In fact, the Mi 8 is now the most accurate GPS-module on the market among smartphones, which can actually be used for land cadastral works, provided that there is adequate software (coftu) for receiving RTK corrections from GSM base stations (Groupe Special Mobile) - channel [11-13].

The urgency of the use of modern electronic gadgets for geodetic measurements is confirmed by the studies conducted by NextNav (2018) [14]. In the course of the study, vertical position accuracy was determined with the help of different models of phones and signals from the installed network of beacons NextNav. The services provided by the NextNav's Metropolitan Beacon System (MBS) allow mobile phones and other devices to reliably determine their location in space, enclosed spaces, and urban environments, where GPS signals can not be obtained.

With regard to special applications for smartphones, for the full use of GNSS technologies, an interesting development is the soft product "GNSS Compare" [15]. This software displays general information about GNSS satellite systems, allows the user to choose the best satellite constellation for precise positioning, compare the performance of signals between different satellite systems, and so on.

Conclusions

As a result of the calculation, we obtained the following results, in particular, with an average square error of the installation of turning points up to 2 cm, a land plot of 0.01 hectares (rectangular – 4 turning points), the error of the area will be 0.8 m^2 , $0.10 \text{ hectares} - 2.56 \text{ m}^2$, $0.25 \text{ ha} - 4.00 \text{ m}^2$, $0.5 \text{ ha} - 5.66 \text{ m}^2$, $1 \text{ ha} - 8.00 \text{ m}^2$, $5 \text{ ha} - 17.9 \text{ m}^2$.

Accurate surveying (determining the position of the turning points of land to 0.02 m), because of its high cost, compared with others, is advisable in cases, where the market value of 1 m² of land is reaching 207.59 m²·USD⁻¹ in determining the boundaries of the land plots with a total area of 0.01 ha; $64.87 \text{ m}^2 \cdot \text{USD}^{-1}$ – land area of 0.10 hectares; $41.52 \text{ m}^2 \cdot \text{USD}^{-1}$ – land area of 0.25 hectares; $29.34 \text{ m}^2 \cdot \text{USD}^{-1}$ – land area of 0.50 hectares; $20.76 \text{ m}^2 \cdot \text{USD}^{-1}$ – land area of 1.00 hectares; $9.28 \text{ m}^2 \cdot \text{USD}^{-1}$ – land area of 5.00 hectares.

We are convinced that in the near future the development of technologies (software) in the field of telecommunications, satellite positioning techniques, GNSS-technologies will allow ordinary landowners to carry out land-cadastral surveys of their land plots (up to 0.5 m) with the help of modern smartphones. This is confirmed by the tendency to use gadgets (special software, in particular, Pix4D, DJI Go, etc.) and unmanned aerial vehicles in the field of land cadastre, which have changed the general pursuit of aerial photography, photogrammetry as a whole. As a result, the existing technologies have allowed users to process the processing the results of photographing automatically with the help of utilities.

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